# Machine Cell Formation Based on a New Similarity Coefficient 

Ibrahim H. Garbie ${ }^{\mathbf{1 *}^{*}}$, Hamid R. Parsaei ${ }^{2}$ and Herman R. Leep ${ }^{3}$<br>${ }^{1}$ Department of Mechanical Engineering, Helwan University, Helwan, Cairo, 11792, EGYPT. ibrahim68@helwan.edu.eg<br>${ }^{2}$ Department of Industrial Engineering, University of Houston, Houston, TX, 77204, USA.<br>${ }^{3}$ Department of Industrial Engineering, University of Louisville, Louisville, KY, 40292, USA.


#### Abstract

One of the designs of cellular manufacturing systems (CMS) requires that a machine population be partitioned into machine cells. Numerous methods are available for clustering machines into machine cells. One method involves using a similarity coefficient. Similarity coefficients between machines are not absolute, and they still need more attention from researchers. Although there are a number of similarity coefficients in the literature, they do not always incorporate the important properties of a similarity coefficient satisfactorily. These important properties include alternative routings, processing time, machine capacity (reliability), machine capability (flexibility), production volume, product demand, and the number of operations done on a machine. The objectives of this paper are to present a review of the literature on similarity coefficients between machines in CMS, to propose a new similarity coefficient between machines incorporating all these important properties of similarity, and to propose a machine cell heuristic approach to group machines into machine cells. An example problem is included and demonstrated in this paper.


Keywords: Cellular manufacturing, Similarity coefficients, Machine cells

## 1. INTRODUCTION

Cluster analysis has been used to study similarity measures and coefficients. Similarity coefficient approaches, which were used in grouping machines into cells, have received considerable attention in the literature. The machine-part incidence matrix is the input for most problems involving machine clustering. The machine-part incidence matrix is a zero-one matrix, [A], where element $a_{i j}=1$ indicates that part j is processed on machine $i$. Although several methods are available in the literature to cluster machines into machine cells, similarity coefficient approaches represent a wellknown methodology in grouping machines, and they are more flexible in incorporating various types of manufacturing data. A wide range of similarity coefficient measures between machines will be explained in the review.

This paper is structured as follows. Section 2 reviews most of the papers published in the area of similarity coefficients between machines. Section 3 presents the proposed similarity coefficient between two machines. The heuristic approach which was used to group machines into machine

[^0]cells is presented in Section 4. Section 5 describes the analytical example. Section 6 presents the conclusion.

## 2. LITERATURE REVIEW

This section presents a comprehensive review of the research work of similarity coefficients between machines are related to the problem of finding similarity between two machines.

Viswanathan (1996) proposed similarity coefficient between two machines for P-median formulation as follows:
$S_{i j}=\sum_{k=1}^{n} \delta\left(a_{i k}, a_{j k}\right)$
$\delta\left(a_{i k}, a_{j k}\right)=2$, if element $a_{i k}=a_{j k}=1$
$\delta\left(a_{i k}, a_{j k}\right)=-1$, if $\quad a_{i k} \neq a_{j k}$
$\delta\left(a_{i k}, a_{j k}\right)=0$, otherwise
$k=$ subscript of part, $k=1, \ldots, n$ (parts)
Viswanathan (1996) used positive and negative values, revealing the extent of similarity as well as dissimilarity. The machines were first clustered by solving for the P-median, and then the parts were assigned to the cells so as to minimize the number of voids inside the cells and the number of ones outside the cells. In this case, he ensured that each cell has at least two parts and two machines.

Jaccard's similarity coefficient equation (McAuley, 1972) is defined as follows:

$$
\begin{equation*}
S_{i j}=\frac{N_{i j}}{N_{i}+N_{j}-N_{i j}} \tag{2}
\end{equation*}
$$

$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$.
$N_{i j} \quad$ number of common parts processed by both machines i and j .
$N_{i} \quad$ number of parts processed by machine $i$ only.
$N_{j} \quad$ number of parts processed by machine $j$ only.

Aljaber et al. (1997) modified Jaccard’s similarity measure (McAuley, 1972) between two machines by subtracting it from its upper bound of 1 , and it can be defined as follows:

$$
\begin{equation*}
S_{i j}=1-\frac{N_{i j}}{N_{i}+N_{j}-N_{i j}} \tag{3}
\end{equation*}
$$

Won and Kim (1997) modified Jaccard's similarity coefficient between two machines to produce a generalized similarity coefficient including alternative routings (process plans) of parts. They defined the generalized machine similarity coefficient between two machines $i$ and $j$ as follows:
$g s c_{i j}=\frac{\delta_{i j}}{\delta_{i}+\delta_{j}-\delta_{i j}}$
$g s c_{i j} \quad$ generalized similarity coefficient between machines $i$ and $j$.
$\delta_{i j}$ number of common parts with multiple process routings processed by both machines $i$ and $j$.
$\delta_{i} \quad$ number of parts with multiple process routing processed by machine $i$ only.
$\delta_{j} \quad$ number of parts with multiple process routing processed by machine $i$ only.

$$
\begin{array}{lll}
\delta_{i}=\sum_{k=1}^{n} \alpha(i, k) & , \quad \delta_{j}=\sum_{k=1}^{n} \alpha(j, k) \\
\alpha(i, k)=1 & \text { if } a_{i k r}=1 \quad \text { for some } r \in R_{k} \\
\alpha(i, k)=0 & \text { otherwise } & \\
\alpha(j, k)=1 & \text { if } a_{j k r}=1 \quad \text { for some } r \in R_{k} \\
\alpha(j, k)=0 & \text { otherwise } & \\
k=1, \ldots, n \text { (parts) } \\
R_{k} \quad \text { set of process routings of part } k & \\
\delta_{i j}=\sum_{k=1}^{n} B(i, j, k) & \\
B(i, j, k)=1 & \text { if } a_{i k r}=a_{j k r} & \text { for some } r \in R_{k}, i \neq j \\
B(i, j, k)=0 & \text { otherwise } &
\end{array}
$$

Yin and Yasuda (2002) modified the similarity coefficient of Won and Kim (1997) by incorporating a sequence ratio ( $S R_{i j}$ ) and machine load ratio ( $M L R_{j}$ ) into equation (4). Then, they defined a new similarity as follows:

$$
\begin{aligned}
& g s c_{i j}= \frac{\delta_{i j}}{\delta_{i}+\delta_{j}-\delta_{i j}} * S R_{i j} * M L R_{j j} \\
& S R_{i j} \quad \text { sequence ratio }=\frac{X_{i j}}{D_{i j}} \\
& M L R_{j j} \quad \text { machine load ratio }=\frac{Y_{i j}}{E_{i j}} \\
& X_{i j} \text { number of actual movements of parts between machines } i \text { and } j \\
& D_{i j} \text { number of possible movements of parts between machines } i \text { and } j \\
& Y_{i j} \text { minimum production volume factor between machine } i \text { and } j \\
& E_{i j} \text { maximum production volume factor between machines } i \text { and } j
\end{aligned}
$$

Yin and Yasuda (2002) suggested also another similarity coefficient between machine cells ( $P$ and $Q)$ as follows:

$$
\begin{equation*}
S_{P Q}=\frac{\sum_{i \in P} \sum_{j \in Q} g s c_{i j}}{N M_{P} \times N M_{Q}} \tag{6}
\end{equation*}
$$

$N M_{P} \quad$ number of machines in cell $P$.
$N M_{Q} \quad$ number of machines in cell $Q$.
Won (2000) suggested two similarity coefficients between two machines for the P-median of machine cell formation under the assumption that each part may be processed by alternative process plans. The first coefficient reflects the extent of similarity between machines $i$ and $j$, and it is defined as follows:
$S_{i j}^{1}=\sum_{k=1}^{n} \alpha(i, j, k)$
if $i \neq j, i, j=1, \ldots, m$
$S_{i j}^{1}=0$ otherwise
$\alpha(i, j, k)=1$, if $a_{i k r}=a_{j k r}=1$ for some $r \in R_{k} k=1, \ldots, n \quad \alpha(i, j, k)=0$, otherwise
The second coefficient reflects the extent of similarity as well as dissimilarity between two machines as follows:
$S_{i j}^{2}=\sum_{k=1}^{n} \beta(i, j, k)$
if $i \neq j, i, j=1, \ldots, m$
$S_{i j}^{2}=0$ otherwise
$\beta(i, j, k)=n \quad$ if $a_{i k r}=a_{j k r}=1$ for some $r \in R_{k}$
$\beta(i, j, k)=-1$ if $a_{i k r} \neq a_{j k r}$ for all $r \in R_{k}$
$\beta(i, j, k)=0$ if otherwise
$n$ number of parts, $m=$ number of machines
Nair and Narendran (1998) defined a new similarity coefficient and incorporated production sequence and product volume to form cells. Then, the similarity coefficient between machines $i$ and $j$ can be described as the ratio of the sum of the moves common to machines $i$ and $j$, and the sum of the total number of moves to and from machines $i$ and $j$ as follows:

$$
\begin{equation*}
S_{i j}(0)=\frac{C_{i}+C_{j}}{t_{i}+t_{j}} \tag{9}
\end{equation*}
$$

$$
\begin{gathered}
t_{i}=\sum_{k=1}^{n} \sum_{p=1}^{n_{i k i}} w_{k} t_{k i p}, t_{j}=\sum_{k=1}^{n} \sum_{p=1}^{n_{k j}} w_{k} t_{k j p}, \\
C_{i}=\sum_{k=1}^{n} \sum_{p=1}^{n_{k i}} w_{k} c_{k i p}, \quad C_{j}=\sum_{k=1}^{n} \sum_{p=1}^{n_{k j}} w_{k} c_{k j p}
\end{gathered}
$$

$t_{i}$ accounts for the total number of moves to and from machine $i$ by components which visit it.
$t_{j} \quad$ accounts for the total number of moves to and from machine $j$ by components which visit it.
$C_{i}$ takes into account the total number of moves to and from machine $i$ made by all components which visit machines $i$ and $j$.
$C_{j}$ takes into account the total number of moves to and from machine $j$ made by all components which visit machines $i$ and $j$.
$t_{k i p}=0 \quad$ if $b_{k i p}=0$
$t_{k i p}=1$ if $b_{k i p}=1$ or $r_{k}$
$t_{k i p}=2$ otherwise
$t_{k j p}=0 \quad$ if $b_{k j p}=0$
$t_{k j p}=1$ if $b_{k j p}=1$ or $r_{k}$
$t_{k j p}=2$ otherwise
$c_{k i p}=0 \quad$ if $b_{k i p}=0$ or $b_{k j p}=0$
$c_{k i p}=1 \quad$ if $b_{k i p}=1$ or $b_{k j p}=1$ or $r_{k}$
$c_{k i p}=2$ otherwise
$c_{k j p}=0 \quad$ if $b_{k i p}=0$ or $b_{k j p}=0$
$c_{k j p}=1$ if $b_{k i p}=1$ or $b_{k j p}=1$ or $r_{k}$
$c_{k j p}=2$ otherwise
$w_{k} \quad$ weight of component $k$
$n$ number of parts, $m=$ number of machines
$r_{k} \quad$ maximum number of operations for component $k$
$b_{k i p} \quad$ operation sequence number if the $k t h(1 \leq k \leq n)$ component visits the $i$ th $(1 \leq i \leq m)$ machine for the $p$ th $\left(1 \leq p \leq n_{k i}\right)$ time, zero
$b_{k j p} \quad$ operation sequence number if the $k$ th $(1 \leq k \leq n)$ component visits the $j$ th ( $1 \leq j \leq m$ ) machine for the $p$ th $\left(1 \leq p \leq n_{k i}\right)$ time, zero
$n_{k i} \quad$ number of times the $k$ th component visits the $i$ th machine
$n_{k i} \quad$ number of times the $k$ th component visits the $j$ th machine

Probhakaran et al. (2002) proposed a combined dissimilarity coefficient measure by mixing a SINE dissimilarity coefficient with the sequence similarity coefficient which was created by Nair and Narendran (1998) (see equation (9)). The SINE dissimilarity coefficient between machines $i$ and $j$ ( $S_{i j}(r)$ ) is defined as the SINE of the angle between the pair of vectors that represent the machines as follows:

$$
\begin{equation*}
S_{i j}(r)=\operatorname{Sin}_{j}(\theta)=\left(1-\operatorname{Cos}_{i j}^{2}(\theta)\right)^{1 / 2} \tag{10}
\end{equation*}
$$

$$
\operatorname{Cos}_{i j}(\theta)=\frac{i . j}{|i| \cdot|j|}
$$

From equation (9) we have $S_{i j}(0)=\frac{C_{i}+C_{j}}{t_{i}+t_{j}}$.
The combined dissimilarity coefficient for a pair of machines $i$ and $j$ is defined as follows:

$$
\begin{equation*}
S_{i j}=\frac{S_{i j}(r)}{j+S_{i j}(0)} \tag{11}
\end{equation*}
$$

Seifoddini and Wolfe (1986) suggested a similarity coefficient. Their similarity coefficient can be described as follows:

$$
\begin{equation*}
S_{i j}=\frac{H A N D}{N O R} \tag{12}
\end{equation*}
$$

NOR and NAND number of non-zero bits in MVO and MVA, respectively

```
MVO MVi OR MVj
MVA MVi AND MVj
    MVi machine vector i
    MVj machine vector j
```

Seifoddini and Djassemi (1991 and 1996) compared the performance of Jaccard's similarity coefficient with the performance of a production-data-based similarity coefficient by using intercellular and intracellular material handling costs and group efficiencies. Jaccard's similarity coefficient is given as follows:

$$
\begin{equation*}
S_{i j}=\frac{\sum_{k=1}^{n} X_{i j k}}{\sum_{k=1}^{n} Y_{i j k}} \tag{13}
\end{equation*}
$$

The production data-based similarity coefficients are given as follows
$S_{i j}=\frac{\sum_{k=1}^{n} V_{k} X_{i j k}}{\sum_{k=1}^{n} V_{k} Y_{i j k}}$
$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$V_{k} \quad$ production volume for part type $k$
$n$ number of part types
$X_{i j k}=1 \quad$ if part type $k$ visits both machines $i$ and $j$
$X_{i j k}=0 \quad$ otherwise
$Y_{i j k}=1 \quad$ if part type $k$ visits either machine $i$ or $j$
$Y_{i j k}=0 \quad$ otherwise
Seifoddini and Tjahana (1999) modified the production-data-based similarity coefficient (equation (14)) between two machines $i$ and $j$ based on the batch size. This similarity coefficient ( $B S_{i j}$ ) can be described as follows:
$B S_{i j}=\frac{\sum_{k=1}^{n}\left(\frac{V_{k}}{b_{k}}\right) * X_{i j k}}{\sum_{k=1}^{n}\left(\frac{V_{k}}{b_{k}}\right) * Y_{i j k}}$
$B S_{i j}$ batch similarity coefficient
$b_{k} \quad$ batch size
Seifoddini (1988) modified the similarity coefficient between machines $i$ and $j$ as follows:
$S_{i j}=\frac{\sum_{k=1}^{n} m_{k} n_{k} X_{k}}{\sum_{k=1}^{n} m_{k} n_{k} Y_{k}}$
$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$n$ number of parts
$m_{k} \quad$ production volume of part type $k$
$n_{k} \quad$ number of times part type $k$ moves between machines $i$ and $j$
$X_{k} \quad$ numerator entry ( 0 or 1) in vector $V_{i j}$
$Y_{K} \quad$ denominator entry (0 or 1) in vector $V_{i j}{ }^{\prime}$
$V_{i j} \quad$ vector containing information on parts visiting both machines $i$ and $j$
$V_{i j}{ }^{\} \quad$ vector containing information on parts visiting either machine $i$ or $j$

Gupta (1991) and Gupta and Seifoddini (1990) created a similarity coefficient between two machines $i$ and $j$ as follows:
$S_{i j}=\frac{\sum_{k=1}^{n}\left[X_{k} t_{i j}^{k}+\sum_{o=1}^{n_{k}} Z_{k o}\right] m_{k}}{\sum_{k=1}^{n}\left[X_{k} t_{i j}^{k}+\sum_{o=1}^{n_{k}} Z_{k o}+Y_{k}\right] m_{k}}$
$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$m_{k} \quad$ planned production volume during a period for part type $k \forall k, k=1, \ldots, n$
$n_{k} \quad$ number of times part type $k$ visits machines $i$ and $j$ consecutively
$X_{k}=1 \quad$ if part type $k$ visits both machines $i$ and $j$
$X_{k}=0 \quad$ otherwise
$Y_{k}=1 \quad$ if part type $k$ visits either machine $i$ or $j$
$Y_{k}=0 \quad$ otherwise
$Z_{k}=1 \quad$ if part type $k$ visits both machines $i$ and $j$ consecutively
$Z_{k}=0 \quad$ otherwise

$$
t_{i j}^{k}=\frac{\min \left(\sum_{o=1}^{n_{k i}} t_{k i}, \sum_{o=1}^{n_{k j}} t_{k j}\right)}{\max \left(\sum_{o=1}^{n_{k j}} t_{k i}, \sum_{o=1}^{n_{k j}} t_{k j}\right)}
$$

$t_{i j}^{k} \quad$ ratio of smaller unit operation time to larger unit operation time for machine pair $i, j$
$n_{k i} \quad$ number of visits part type $k$ makes to machine $i$
$n_{k j} \quad$ number of visits part type $k$ makes to machine $j$
$t_{k i} \quad$ unit operation time for part type $k$ on machine $i$ during oth visit
$t_{k j} \quad$ unit operation time for part type $k$ on machine $j$ during oth visit
Seifoddini (1989) proposed a similarity coefficient to eliminate improper machine assignment by assigning a higher weight to parts having common operations on both machines. This similarity coefficient is defined as follows:
$S_{i j}=\frac{\sum_{k=1}^{n} f_{b k} X_{i j k}}{\sum_{k=1}^{n} f_{b k} X_{i j k}+\sum_{k=1}^{n} f_{e k} Y_{i j k}}$
$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$n$ total number of parts
$X_{i j k}=1 \quad$ if part type $k$ visits both machines $i$ and $j$
$X_{i j k}=0 \quad$ otherwise
$Y_{i j k}=1 \quad$ if part type $k$ visits either machine $i$ or $j$
$Y_{i j k}=0 \quad$ otherwise
$f_{b k} \quad$ weighting factor for parts visiting both machines $i$ and $j$
$f_{e k} \quad$ weighting factor for parts visiting either machine $i$ or $j$, but not both

Gupta (1993) modified his previous similarity coefficients Gupta (1991) and Gupta and Seifoddini (1990) to incorporate an alternative routing sequence in addition to production volumes and operation times for each part in the formation of part families and machine cells as follows:
$S_{i j}=\frac{\sum_{k=1}^{n}\left[\sum_{r=1}^{r_{k}}\left(X_{k r} t_{k r}+n_{k r}\right) P_{k r}\right] m_{k}}{\sum_{k=1}^{n}\left[\sum_{r=1}^{r_{k}}\left(X_{k r} t_{k r}+n_{k r}+Y_{k r}\right) P_{k r}\right] m_{k}}$
$r_{k} \quad$ number of alternative routes for part type $k$
$P_{k r} \quad$ usage factor of route r for part type $k$
$n_{k r} \quad$ number of trips part type $k$ makes between machines $i$ and $j$ for consecutive operations on the $r$ th route

Lee et al. (1997) and Luong et al. (2001) proposed a similarity coefficient between machines. They called it a machine chain similarity coefficient $\left(M C S_{i j}\right)$ between machines $i$ and $j$ depending on the processing sequences, production volumes, and alternative routing.
$M C S_{i j}=\frac{\sum_{l=1}^{m}\left(\min \left(\sum_{k=1}^{n} P_{i l}^{k}, \sum_{k=1}^{n} P_{j l}^{k}\right)\right)}{\sum_{l=1}^{m} \sum_{k=1}^{n}\left(V_{k l}+V_{k l}^{\prime}\right)}$
$V_{k l} \quad$ number of units of $k$ coming from machine $l$
$V_{k l}^{\prime} \quad$ number of units of part type $k$ going to machine $l$
$n$ number of parts, $m=$ number of machines
$P_{i l}^{k}=\frac{\# \text { of units of part } k \text { moved between machines } i \text { and } l \text { if } i \neq l}{\# \text { of units of part } k \text { moved between machines } \text { i and } l \text { if } i=l}$
$P_{j l}^{k}=\frac{\# \text { of unitsof partk movedbetweermachinesj andl if } j \neq l}{\# \text { of unitsof partk movedbetweermachinesj andl if } j=l}$

Mosier (1989) developed three different types of similarity coefficients between machines. The first similarity coefficient between machines $i$ and $j$ can be described as follows:

$$
\begin{equation*}
S_{i j}=\frac{a_{i j}-b_{i j} c_{i j}}{a_{i j} d_{i j}+b_{i j} c_{i j}} \tag{21}
\end{equation*}
$$

The second similarity coefficient is as follows:

$$
\begin{equation*}
S_{i j}=\frac{\left(a_{i j}+d_{i j}\right)-\left(b_{i j}+c_{i j}\right)}{\left(a_{i j}+d_{i j}\right)+\left(b_{i j}+c_{i j}\right)} \tag{22}
\end{equation*}
$$

The last similarity coefficient is as follows:

$$
\begin{equation*}
S_{i j}=\frac{a_{i j}+\left(a_{i j} d_{i j}\right)^{1 / 2}}{a_{i j}+b_{i j}+c_{i j}+\left(a_{i j} d_{i j}\right)^{1 / 2}} \tag{23}
\end{equation*}
$$

$a_{i j} \quad$ count of parts processed on machines $i$ and $j$
$d_{i j} \quad$ number of parts processed on neither machine $i$ or $j$
$b_{i j}$ and $c_{i j}$ number of parts processed on machine $i$ only, and machine $j$ only, respectively

Islam and Sarker (2000) modified similarity coefficient (23) to form machine cells (equation (23)) by adding the new term $d_{i j}$ in the denominator to form cohesive cells. It is defined as follows:

$$
\begin{equation*}
S_{i j}=\frac{a_{i j}+\left(a_{i j} d_{i j}\right)^{1 / 2}}{a_{i j}+b_{i j}+c_{i j}+d_{i j}+\left(a_{i j} d_{i j}\right)^{1 / 2}} \tag{24}
\end{equation*}
$$

Gunasingh and Lashkari (1989) proposed a similarity coefficient between two machines based on the similarity in the processing of parts. The similarity coefficient $S_{i j}$ between machines $i$ and $j$ can be described as follows:
$S_{i j}=\frac{\sum_{k \in C p_{i j}}\left[N C T_{k i}+N C T_{k j}\right]}{\sum_{k}^{n}\left[N C T_{k i}+N C T_{k j}\right]}$
$N C T_{k i}$ number of common tools between part $k$ and machine $i$
$N C T_{k j} \quad$ number of common tools between part $k$ and machine $j$
$C P_{i j} \quad$ set of parts requiring both machines $i, j$
$n$ number of parts

Waghodekar and Sahu (1984) proposed three similarity coefficients between machines $i$ and $j$. The first one was for the additive type, and it will be described as follows:

$$
\begin{equation*}
S C_{i j}=\frac{N C C_{i j}}{T N C_{i}+T N C_{j}-N C C_{i j}} \tag{26}
\end{equation*}
$$

$N C C_{i j}$ number of common components using both machines $i$ and $j$
$T N C_{i}$ total number of components using machine $i$
$T N C_{j} \quad$ total number of components using machine $j$
The second similarity coefficient was used for product type based on the total number of components processed by each machine $i$ and machine $j$ as follows:

$$
\begin{equation*}
P S C_{i j}=\frac{N C C_{i j} \times N C C_{i j}}{T N C_{i} \times T N C_{j}} \tag{27}
\end{equation*}
$$

The last coefficient was based on total flow of common components processed by a machine as follows:

$$
\begin{equation*}
S C T F_{i j}=\frac{N C C_{i j} \times N C C_{i j}}{T F C_{i} \times T F C_{j}} \tag{28}
\end{equation*}
$$

$T F C_{i}$ total flow of common components processed by machine $i$
$T F C_{j}$ total flow of common components processed by machine $j$

$$
T F C_{i}=\sum_{k=1}^{n} N C C_{i j}, T F C_{j}=\sum_{k=1}^{n} N C C_{i j} \text { for } i \# j
$$

Leem and Chen (1996) used a similarity coefficient between two machines to form machine cells based on a fuzzy set approach. The new similarity coefficient can be described as follows:

$$
\begin{aligned}
& S_{i j}=\frac{\sum_{k=1}^{n}\left(\mu_{i k} \cap \mu_{j k}\right)}{\sum_{k=1}^{n}\left(\mu_{i k} \cup \mu_{j k}\right)} \\
& 0 \leq \mu_{i k} \leq 1 \text { and } 0 \leq \mu_{j k} \leq 1 \\
& \sum_{k=1}^{n} \mu_{i k} \succ 0 \text { for } i=1, \ldots, n ; \sum_{k=1}^{n} \mu_{j k} \succ 0 \\
& \text { for } j=1, \ldots, n ; \text { for i and } j=1, \ldots, n \\
& \quad n \quad \text { number of parts }
\end{aligned}
$$

Ponnambalam and Aravindan (1994) used a similarity coefficient between two machines $i$ and $j$ as follows:

$$
\begin{align*}
& S_{i j}=\sum_{k=1}^{n} d_{k}  \tag{30}\\
& d_{k}=1 \\
& d_{k}=0 \\
& \text { if } a_{i k}=a_{j k} \\
& S_{j j}=0
\end{align*} \quad \text { if } k=\text { index for part, } k=1, \ldots, n .
$$

Luong (1993) proposed a similarity coefficient which considered the similarity between machines cells rather than individual machines. The new similarity coefficient will be described as follows:
$S_{P Q}=\frac{\sum_{i=1}^{m_{q}} \sum_{j=1}^{m_{p}} X_{i} Y_{j}}{\min (n, m)}$
$S_{P Q} \quad$ similarity coefficient between machine cells $P$ and $Q$.
$X_{i} Y_{j}=1$ if $X_{i}=Y_{j} ; X_{i} Y_{j}=0$, if $X_{i} \neq Y_{j}$
$\min \left(m_{p}, m_{q}\right)=m_{p}$, if $m_{p}<m_{q} ; \min \left(m_{p}, m_{q}\right)=m_{q}$ if $m_{p}>m_{q}$
$m_{p} \quad$ number of machines in cell $P$
$m_{q} \quad$ number of machines in cell $Q$
Nazarlo and Ramirez (2000) proposed a new similarity coefficient between two machines. The proposed similarity coefficient can be defined as follows:
$S_{i j}=\frac{1}{4}\left(\Pi_{i}-\Pi_{j}\right) *\left(1+e^{-\delta_{i j}}\right)$
$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$\Pi_{i}$ proportion of common time that parts spend on machine $i$

$$
\Pi_{i}=\frac{\sum_{k \in A} P_{i k}}{\sum_{k \in B} P_{i k}}
$$

$\Pi_{j} \quad$ proportion of common time that parts spend on machine $j$

$$
\Pi_{j}=\frac{\sum_{k \in A} P_{i k}}{\sum_{k \in C} P_{i k}}
$$

A set of parts that are processed on machines $i$ and $j$
B set of parts that are processed on machine $i$

$$
\begin{aligned}
\text { C } & \text { set of parts that are processed on machine } j \\
P_{i k} & \text { processing time of part } k \text { on machine } i \\
\delta_{i j} & \text { distance proportion between machines } i \text { and } j \\
\delta_{i j} & =\frac{h_{i j}}{H} \\
H & \text { max }\left\{h_{i j}\right\}, \text { if } h_{i j} \neq 0 \\
H=1 & \text { if } h_{i j}=0 \\
h_{i j} & \text { distance between machines } i \text { and } j \text { (assume locations of machines } i \text { and } j \text { are known). }
\end{aligned}
$$

Chang and Lee (2000) suggested a similarity coefficient between two machines $i$ and $j$ as follows:

$$
\begin{array}{ll}
S_{i j}=\sum_{k=1}^{N}\left(1-\left|a_{i k}-a_{j k}\right|\right) & \text { if } i \neq j  \tag{33}\\
S_{i j}=0, & \text { if } i=j
\end{array}
$$

Lozano et al. (2001) suggested a similarity coefficient between two machines $i$ and $j$ as follows:

$$
\begin{equation*}
S_{i j}=n_{i j}+n_{j i} \tag{34}
\end{equation*}
$$

$n_{i j} \quad$ total number of part movements from machine $i$ to machine $j$
$n_{j i}$ total number of part movements from machine $j$ to machine $i$
$n_{i j}=\sum_{k=1}^{n} \sum_{l}^{o_{i}} D_{k} \delta_{i j k l}$
$D_{k} \quad$ demand for part type k
$\delta_{i j k l}=1 \quad$ if $m_{k l}=1$
$\delta_{i j k l}=0 \quad$ otherwise
$m_{k l}$ machine on which operation l of part type $k$ is performed
Yasuda and Yin (2001) proposed a system representing the dissimilarity of a pair of machine groups and part families based on the calculation of an average voids value (AVV).
$A V V=\frac{\sum_{m=1}^{M_{i}}\left(v c_{i m}{ }^{j}-v c_{i m}\right)}{M_{i}}+\frac{\sum_{n=1}^{M_{j}}\left(v c_{j n}{ }^{i}-v c_{j n}\right)}{M_{j}}$
$c_{i}$ machine group i in the problem
$c_{i m}$ machine $m$ of $c_{i}$
$c_{i m}{ }^{j} \quad$ machine m of $c_{i}$ in $c_{i}{ }^{j}$
$v c_{i m} \quad$ number of voids produced by machine m of $c_{i}$

```
    \(v c_{i m}{ }^{j} \quad\) number of voids produced by machine \(m\) of \(c_{i}\) in \(c_{i}{ }^{j}\)
    \(v c_{j m} \quad\) number of voids produced by machine \(m\) of \(c_{j}\)
    \(v c_{j m}^{i} \quad\) number of voids produced by machine \(m\) of \(c_{j}\) in \(c_{j}{ }^{i}\)
\(c_{i}{ }^{j}=c_{j}{ }^{i} \quad\) (the machine group formed by \(c_{i}\) and \(c_{j}\) )
    \(M_{i}\) number of machines in \(c_{i}\)
    \(M_{j} \quad\) number of machines in \(c_{j}\)
    \(m\) subscript of machine in \(c_{i}\)
    \(n\) subscript of machine in \(c_{j}\)
```

Shaferm and Rogers (1993) suggested a similarity coefficient between two machines as follows:

$$
\begin{equation*}
\text { MAXSC }_{i j}=\max \left[\frac{M_{i j}}{M_{i}}, \frac{M_{i j}}{M_{j}}\right] \tag{36}
\end{equation*}
$$

$M_{i j} \quad$ number of components that visit both machine types $i$ and $j$
$M_{i} \quad$ number of components that visit machine type $i$
$M_{j} \quad$ number of components that visit machine type $j$

## 3. THE PROPOSED SIMILARITY COEFFICIENT BETWEEN MACHINES

A comprehensive new similarity coefficient between machines will be created by considering alternative routings, processing time, machine capacity (reliability), machine capability (flexibility), production volume, product (part) demand, and number of operations done on each machine (figure 1). A relationship between machines can be calculated by using their similarity coefficient. The relationship between machines usually ranges from 0 to 1 , as most researchers range as a function of the definition of a coefficient. As the value of the similarity coefficient approaches 1 , the two machines become more similar. If this value is equal to 0 , there is no similarity between them. The main objective for creating the new similarity coefficient between machines is to take both direct and indirect relations between them into consideration.

The mathematical expression for the new similarity coefficient between machines i and j , which was based on machine capacity, machine flexibility (maximum number of operations available per machine), part (product) volume and demand, number of operations performed by machines, and processing time, will be explained as follows (see equations (37) and (38)).

## Assumptions:

The model assumes that the following information has been collected and screened for accuracy or specified by the user.

1. The processing times for all part type operations with associated process plans on different machine types are known.
2. The capacity of each machine type is known and constant over time.
3. The capability of each machine type is also known and constant over time.
4. Each machine type can perform one or more operations.
5. The production volume of each part type in a specific period is known.
6. The demand for each part type in the specific period is also known.
7. The production volume per part is greater than part demand.


Figure 1. Issues that will be used to create a new similarity coefficient between machines.
or

$$
\begin{equation*}
S_{i j}=\frac{\sum_{\substack{k=1 \\ \text { and } \\ r \in k j}} \sum_{r \in k i}^{R}\left[\max \left(\frac{t_{k i r}}{C_{i}} \times \frac{n_{o_{i}}}{N_{o_{i_{\max }}}}, \frac{t_{k j r}}{C_{j}} \times \frac{n_{o_{j}}}{N_{o_{j_{\max }}}}\right) X_{i j k r}\right]\left(B S_{k}\right)}{\sum_{\substack{n_{X_{i j k r}}}}^{n_{k=1}} \sum_{\substack{r \in k i \\ \text { and } \\ r \in k j}}^{R}\left[\max \left(\frac{t_{k i r}}{C_{i}} \times \frac{n_{o_{i}}}{N_{o_{i_{\max }}}}, \frac{t_{k j r}}{C_{j}} \times \frac{n_{o_{j}}}{N_{o_{j_{\max }}}}\right) X X_{i j k r}\right]\left(B S_{k}\right)+\sum_{\substack{k=1+n_{X_{i j k r}}}}^{\substack{r=k i \\ o r \\ r \in k j}}\left[\left(\frac{t_{k i r}}{C_{i}} \times \frac{n_{o_{i}}}{N_{o_{i_{\max }}}} O R \frac{t_{k j r}}{C_{j}} \times \frac{n_{o_{j}}}{N_{o_{j_{\max }}}}\right) Y_{i j k r}\right]\left(B S_{k}\right)} \tag{38}
\end{equation*}
$$

$S_{i j} \quad$ similarity coefficient between machines $i$ and $j$
$t_{k i r} \quad$ processing time part $k$ takes on machine $i$ including setup time with process plan $r$
$t_{k j r} \quad$ processing time part $k$ takes on machine $j$ including setup time with process plan $r$
$n_{o_{i}} \quad$ number of operations done on machine $i$
$n_{o_{j}} \quad$ number of operations done on machine $j$
$N_{o_{i_{\max }}} \quad$ maximum number of operations available on machines $i$
$N_{o_{j_{\max }}} \quad$ maximum number of operations available on machine $j$
$C_{i}$ capacity of machine $i$
$C_{j} \quad$ capacity of machine $j$
$V_{k} \quad$ part volume of part type $k$ per period
$D_{k} \quad$ part demand of part type $k$ per period
$B S_{k} \quad$ batch size of part $k$
$X_{i j k r}=1 \quad$ if part type $k$ visits both machines $i$ and $j$ with process plan $r$
$X_{i j k r}=0 \quad$ otherwise
$Y_{i j k r}=1 \quad$ if part type $k$ visits either machine $i$ or machine $j$ with process plan $r$
$Y_{i j k r}=0 \quad$ otherwise
$\mathrm{k}=1, \ldots, n$ (parts), $l=1, \ldots, m$ (machines), $r=1, \ldots, R$ (routings)
$R \quad$ number of part routings that can be processed on both machines $i$ and $j$
$R^{\} \quad$ number of part routings that can processed on either machine $i$ or machine $j$
$m$ number of machines in the machine-part incidence matrix.
$n \quad$ number of parts $R$ in the machine-part incidence matrix.
$n_{X_{i j l r}} \quad$ number of parts that can visit both machines $i$ and $j$ with process routings $r$
$\frac{t_{k i r}}{C_{i}}$ fraction of processing time which part $k$ will take from the capacity of machine $i$
$\frac{t_{k j r}}{C_{j}}$ fraction of processing time which part $k$ will take from the capacity of machine $j$
$\frac{n_{o_{i}}}{N_{o_{i_{\max }}}}$ number of operations done on machine $i$ with respect to the maximum number of operations available on that machine. This term represents the flexibility of machine $i$
$\frac{n_{o_{j}}}{N_{o_{j_{\max }}}}$ number of operations done on machine $j$ with respect to the maximum number of operations available on that machine. This term represents the flexibility of machine $j$
$\frac{V_{k}}{D_{k}} \quad$ ratio of production volume rate to demand per part

## 4. HEURISTIC APPROACH FOR MACHINE CELL FORMATION

Machines are assigned to machine cells based on our new similarity coefficient. The procedure to group machines into cells is given by the following steps:

Step 1: Check the Machine Work Load (MWL) of each machine type capacity ( $C_{i}, \ldots, C_{m}$ ) to produce all production volumes for all parts $\left(V_{1}, \ldots, V_{n}\right)$ by these machines in the machinepart incidence matrix. The MWL of machine $i$ is based on production volumes and processing times of all parts assigned to machine $i$. The equation for computing the MWL for machine $i$ is shown as follows:

$$
\begin{equation*}
M W L_{i}=\sum_{k=1}^{n}\left(\sum_{r_{1}, r_{2}, r_{r} \in k i}^{k_{i r_{r}}} \max \left(t_{k i_{r_{1}}} V_{k}+t_{k i_{r_{2}}} V_{k}+\ldots+t_{k i_{r_{r}}} V_{k}\right)\right) \tag{39}
\end{equation*}
$$

Step 2: Compute the similarity coefficient matrix between all machine pairs according to equations (37) and (38).

Step 3: Determine the desired number of machines cells (NMC ) by the following equation:

$$
N M C \geq \frac{m}{m_{\max }}
$$

$m$ number of machines in machine-part incidence matrix.
$m_{\max }$ pre-determinable maximum number of machines in the machine cell (at least two machines per cell)

Step 4: Select the largest similarity coefficient between machine i and machine ( $j, \ldots, m$ ) from the similarity coefficient matrix in each row directly.

Step 5: Sort the similarity coefficients from highest to lowest value and record the values of $S_{h}$ and the corresponding sets of $m_{h}\{i, j\}$, where $h$ represents the level of the similarity value.

Step 6: Start forming the first machine cell $M C_{1}$ by selecting the highest similarity coefficient. value $S_{1}$. Then, this pair of machines $m_{1}\{i, j\}$ will be clustered into the first machine cell.

Step 7: Check the minimum machine cell size constraint (at least two machines per cell).
Step 8: Increase the value of $h(h=2, \ldots, H)$.

Step 9: If $m_{h} \cap M C_{1} \neq 0$. Then, modify $M C_{1}$ by the new $M C_{1}=M C_{1} \cup m_{h}$.

Otherwise, form a new machine cell $M C_{n}(n=2, \ldots, N M C)$.

Step 10: If any set $m_{h}$ intersects two cells $M C_{I}$ and $M C_{J}$, then, discard the corresponding $S_{h}$ and go back to Step 8.

Step 11: Check for the maximum number of machines allowed in a machine cell.
If the number of machines in this machine cell does not exceed the desired number of machines, then, add to this cell.
Otherwise, stop adding to this cell and go back to Step 8.
Step 12: If all the machines have not been assigned to machine cells, go back to Step 8. Otherwise, go to Step 13.

Step13: If the number of machine cells formed exceeds the desired number of machine cells $N M C$, join two machine cells into one machine cell. All these steps will be shown in Figures 2 and 3.

## 5. ANALYTICAL EXAMPLE

In order to demonstrate the proposed approach, the following numerical example will illustrate the procedure, including the similarity coefficients and formation of machines into machine cells. It is composed of 10 types of machines and seven types of parts with different process plans. The incidence matrix between machines and parts is presented in table 1. The part information including operation sequence and processing times for each process plan, and production volume and part demand is also presented in table 2. Information about machine availability, including the capacities of the machines, number of operations that will be done on machines, and maximum number of operations available on machines, is shown in table 3.

Table 1. Incidence matrix between machines and parts.



Figure 2. Flow chart of grouping machines into machine cells (Part 1).


Figure 2. Flow chart of grouping machines into machine cells (Part 2).

Table 2. Parts information.

| Part Type |  | Operation Sequence | Processing Time (Minutes) | Production Volume | Number of Operations per Part | Part <br> Demand |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P1 | r11 | M1-M4-M5-M7- | 2.0-3.2-0.9-2.5-0.6 |  | 5 |  |
|  |  | M10 |  | 2000 |  | 1800 |
|  | r12 | M2-M3-M6-M8-M9 | $\begin{aligned} & 2.7-3.0-\quad 4.0-1.35- \\ & 0.71 \end{aligned}$ |  | 5 |  |
| P2 | r21 | $\begin{aligned} & \text { M1-M2-M4-M5-M6- } \\ & \text { M10 } \end{aligned}$ | $\begin{aligned} & 3.0-2.5-0.8-1.1-1.7- \\ & 2.35 \end{aligned}$ | 2100 | 6 |  |
|  | r22 | M1-M3-M4-M6-M9 | 2.5-1.8-2.2-3.1-2.11 |  | 5 | 2000 |
|  | r23 | $\begin{aligned} & \text { M2-M3-M5-M7-M8- } \\ & \text { M10 } \end{aligned}$ | $\begin{aligned} & 2.0-1.2-3.0-1.3-4.4- \\ & 1.8 \end{aligned}$ |  | 6 |  |
| P3 | r31 | M1-M4-M7-M8-M9 | 1.1-1.8-2.6-1.5-1.35 |  | 5 |  |
|  | r32 | $\begin{aligned} & \text { M3-M5-M8-M9- } \\ & \text { M10 } \end{aligned}$ | $\begin{aligned} & 3.6-\quad 0.6-\quad 2.6-\quad 0.11- \\ & 1.93 \end{aligned}$ | 900 | 5 | 650 |
| P4 | r41 | M2-M4-M6-M9 | 3.0-3.65-0.5-1.95 | 2400 | 4 | 2000 |
| P5 | r51 | M3-M6-M7-M8- | 4.4- 2.83-1.1- 2.32- |  | 5 |  |
|  |  | M10 | 2.0 | 1800 |  | 1700 |
|  | r52 | M1-M2-M7-M9 | 4.83-0.9-0.7-2.28 |  | 4 |  |
| P6 | r61 | M2-M4-M7-M10 | 1.6-2.1-0.9-1.8 | 1900 | 4 | 1700 |
|  | r62 | M1-M8-M9 | 2.0-2.3-0.7 |  | 3 |  |
| P7 | r71 | M3-M8-M10 | 2.0-3.1-3.0 | 2700 | 3 | 2100 |
|  | r72 | M2-M4-M6-M9 | 0.8-1.9-2.5-4.2 |  | 4 |  |

Table 3. Machine information.

| Machine <br> Type | Capacity of <br> machine <br> (Hours) | Number of <br> Operations done on <br> machine <br> $\left(n_{o}\right)$ | Maximum number of operations <br> available on machine <br> $\left(N_{\text {max }}\right)$ |
| :---: | :---: | :---: | :---: |
| 1 | 2400 | 6 | 6 |
| 2 | 2000 | 7 | 7 |
| 3 | 2300 | 6 | 6 |
| 4 | 3000 | 7 | 10 |
| 5 | 1800 | 4 | 4 |
| 6 | 1900 | 6 | 9 |
| 7 | 2700 | 6 | 8 |
| 8 | 1300 | 7 | 10 |
| 9 | 2500 | 8 | 9 |
| 10 | 2100 | 7 | 10 |

### 5.1. Similarity Coefficient between Machines

The similarity coefficient between machines has been coded in the C programming language and executed on a Pentium IV processor. The result of similarity coefficients between machines is illustrated in table 4.

### 5.2. Machine Cells Formation

Step 1: Check the capacity of each machine type (availability of time per machine) to produce all parts that require processing on the machine.

For machine one (M1), the capacity for M1 equals 2400 hours.
The total consumed time taken from M1 will be calculated as follows:

$$
\frac{1}{60}\left[\begin{array}{l}
2(2000)+\max [3.0(2100)+ \\
2.5(2100)+1.1(900)+ \\
4.83(1800)+2.0(1900)]
\end{array}\right]=\frac{23,784}{60}=396.4 \text { hours }
$$

The slack of time on machine (M1) is 2400-396 = 2004 hours. So, M1 is OK. The slack of time on machine (M2) is 2000-412 $=1588$ hours. So, M2 is OK. The slack of time on machine (M3) is $2300-439=1861$ hours. So, M3 is OK. The slack of time on machine (M4) is $3000-509=2491$ hours. So, M4 is OK. The slack of time on machine (M5) is $1800-144=1656$ hours. So, M5 is OK. The slack of time on machine (M6) is 1900-453 $=1447$ hours. So, M6 is OK. The slack of time on machine (M7) is 2700-229 = 2471 hours. So, M7 is OK. The slack of time on machine (M8) is $1300-440=860$ hours. So, M8 is OK. The slack of time on machine (M9) is 2500-475 $=2025$ hours. So, M9 is OK. The slack of time on machine (M10) is $2100-383=1716$ hours. So, M10 is OK.

The capacities of all machines are satisfy to all production volumes for all parts.
Step 2: Compute the similarity coefficient matrix between all machines according to the similarity coefficient (37).

Table 4. Similarity coefficients between machines.

|  | M1 | M2 | M3 | M4 | M5 | M6 | M7 | M8 | M9 | M10 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |
| M1 | 0.0000 | 0.1856 | 0.0739 | 0.4613 | 0.2422 | 0.2219 | 0.5072 | 0.1501 | 0.4751 | 0.1996 |
| M2 |  | 0.0000 | 0.1816 | 0.4218 | 0.3305 | 0.5031 | 0.2510 | 0.2560 | 0.5466 | 0.3057 |
| M3 |  |  | 0.0000 | 0.0698 | 0.3928 | 0.4293 | 0.2458 | 0.7618 | 0.3653 | 0.6190 |
| M4 |  |  |  | 0.0000 | 0.2308 | 0.3287 | 0.5097 | 0.0779 | 0.3326 | 0.3339 |
| M5 |  |  |  |  | 0.0000 | 0.0751 | 0.4640 | 0.3568 | 0.0511 | 0.6015 |
| M6 |  |  |  |  |  | 0.0000 | 0.1312 | 0.1909 | 0.6068 | 0.1942 |
| M7 |  |  |  |  |  |  | 0.0000 | 0.3954 | 0.2516 | 0.4381 |
| M8 |  |  |  |  |  |  |  | 0.0000 | 0.3363 | 0.6110 |
| M9 |  |  |  |  |  |  |  |  | 0.0000 | 0.0821 |
| M10 |  |  |  |  |  |  |  |  |  | 0.0000 |

Step 3: Determine the desired number of machine cells, NMC. The maximum number of machines assigned to cells ranged from 3 to 7 machines (Wilhelm et al. 1998) and from 5 to 10 machines (Ramabhatta and Nagi 1998). Four machines per cell are recommended for easy management and control.
$N M C \geq \frac{10}{4} \geq 2.5$. Therefore, the number of machine cells can start with three cells.
Three machine cells will be chosen.
Step 4: Select the largest similarity coefficient between machine $i$ and machine ( $j, \ldots, m$ ) from Table 4 as follows:

| $m_{1}-m_{7}$ | 0.5072 |
| :--- | :--- |
| $m_{2}-m_{9}$ | 0.5466 |
| $m_{3}-m_{8}$ | 0.7618 |
| $m_{4}-m_{7}$ | 0.5097 |
| $m_{5}-m_{10}$ | 0.6015 |
| $m_{6}-m_{9}$ | 0.6068 |
| $m_{7}-m_{10}$ | 0.4381 |
| $m_{8}-m_{10}$ | 0.6110 |
| $m_{9}-m_{10}$ | 0.0821 |

Step 5: Sort the similarity coefficients from the highest to lowest value and record the values of $S_{h}$ and the corresponding sets of $m_{h}\{i, j\}$

| $H$ | $m_{h}\{i, j\}$ | $S_{h}$ |
| :---: | :--- | :---: |
| 1 | $m_{3}-m_{8}$ | 0.7618 |
| 2 | $m_{8}-m_{10}$ | 0.6110 |
| 3 | $m_{6}-m_{9}$ | 0.6068 |
| 4 | $m_{5}-m_{10}$ | 0.6015 |
| 5 | $m_{2}-m_{9}$ | 0.5466 |
| 6 | $m_{4}-m_{7}$ | 0.5097 |
| 7 | $m_{1}-m_{7}$ | 0.5072 |
| 8 | $m_{7}-m_{10}$ | 0.4381 |

Step 6: For $S_{1}=0.7618$ (between Machines 3 and 8).

Then, $M C_{1}=\{\mathbf{3}, \mathbf{8}\}$

Step 7: Check the minimum machine cell size constraint (at least two machines per cell).
Step 8: $S_{2}=0.6110$ (between Machines 8 and 10).
$m_{2}=\{8,10\}$
Step 9: There is an intersection between Machine 8 and $M C_{1}$.
The new machine cell is $M C_{1} \cup m_{2}$.
Then, the revised machine cell $M C_{1}=\{\mathbf{3}, \mathbf{8}, \mathbf{1 0}\}$
$S_{3}=0.6068$ (between Machines 6 and 9)
$m_{3}=\{6,9\}$ and $M C_{1} \cap m_{3}=0$
$S_{3}$ does not intersect with $M C_{1}$
Then, form a new machine cell $M C_{2}=\{6,9\}$
$S_{4}=0.6015$ (between Machines 5 and 10)
$m_{4}=\{5,10\}$
There is an intersection between Machine 10 and $M C_{1}$, but there is no intersection with $M C_{2}$.
The new machine cell is $M C_{1} \cup m_{4}$.
Then, the revised machine cell
$M C_{1}=\{\mathbf{3}, \mathbf{5}, \mathbf{8}, 10\}$
Step 10: Check for the maximum number of machines a machine cell.
Machine Cell 1 contains four machines. Therefore, no more machines are added to $M C_{1}$.
$S_{5}=0.5466$ (between Machines 2 and 9)
$m_{5}=\{2,9\}$
There is an intersection between Machine 9 and $M C_{2}$, but this is no intersection with $M C_{1}$. The new machine cell is $M C_{2} \cup m_{5}$.
Then, the revised machine cell $M C_{2}=\{\mathbf{2}, \mathbf{6}, \mathbf{9}\}$
$S_{6}=0.5092$ (between Machines 4 and 7)
$m_{6}=\{4,7\}, M C_{1} \cap m_{6}=0$, and $M C_{2} \cap m_{6}=0$
There is no intersection between Machines 4 or 7 with either $M C_{1}$ or $M C_{2}$.
Then, forms a new machine cell $M C_{3}=\{4,7\}$
$S_{7}=0.5072$ (between Machines 1 and 7)
$m_{7}=\{1,7\}$
There is an intersection between Machine 7 and $M C_{3}$, but this is no intersection with $M C_{1}$ or $M C_{2}$. The new machine cell is $M C_{3} \cup m_{7}$.
Then, the revised machine cell $M C_{3}=\{1,4,7\}$
Step 11: All the machines have been assigned to machine cells. Stop.

Machine Cells are as follows:
$M C_{1}=\{3,5,8$, and $\mathbf{1 0 \}}$
$M C_{2}=\{2,6$, and 9$\}$
$M C_{3}=\{1,4$, and 7$\}$

## 6. CONCLUSIONS

This paper proposed a new similarity coefficient for grouping machines into machine cells. Similarity coefficients between machines were reviewed through this paper. These similarity coefficients show that there are several factors or issues to be used in determining the similarity between machines. Some of them concentrated on the machine-part incidence matrix, and the rest of them depend on one or two production and/or flexibility issues like production volume, operation sequence, part demand, and number of intercellular moves. This variation will lead to suggest a new comprehensive similarity coefficient between machines including the most important production and flexibility issues. The main difference between the proposed similarity coefficient and those which already existed in the literature is the lack of them to incorporate all the real world issues. The results in table 4 showed how each value of the similarity coefficient is different. The heuristic based similarity approach was used to group machines into machine cells.

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[^0]:    * Corresponding Author

